Algorithms
4.1 Breadth-First Search Demo

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http://algs4.cs.princeton.edu

## Breadth-first search demo

Repeat until queue is empty:

- Remove vertex $v$ from queue.
- Add to queue all unmarked vertices adjacent to $v$ and mark them.

tinyCG.txt
V

graph G


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queue $\quad$| $\mathbf{v}$ | edgeTo[] | distTo[] |
| :---: | :---: | :---: |
| 0 | - | 0 |
| 1 | - | - |
| 2 | - | - |
| 3 | - | - |
| 4 | - | - |
| 5 | - | - |

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| :---: | :---: | :---: | :---: |
|  | 0 | - | 0 |
| 1 | - | - |  |
|  | 2 | - | - |
| 3 | - | - |  |
| 4 | - | - |  |
|  |  | - | - |
|  |  |  |  |
| 0 |  |  |  |

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queue | v | edgeTo[] | distTo[] |
| :---: | :---: | :---: |
| 0 | - | 0 |
| 1 | - | - |
| 2 | 0 | 1 |
| 3 | - | - |
| 4 | - | - |
| 5 | - | - |

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| :---: | :---: | :---: | :---: |
|  | 0 | - | 0 |
|  | 1 | 0 | 1 |
| 2 | 0 | 1 |  |
| 3 | - | - |  |
| 4 | - | - |  |
|  | 5 | - | - |
|  |  |  |  |
| 2 |  |  |  |
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|  | 2 | 0 | 1 |
|  | 3 | - | - |
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|  | 1 | 0 | 1 |
|  | 2 | 0 | 1 |
| 5 | 3 | - | - |
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| 2 |  |  |  |

0 done

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|  | 0 | - | 0 |
|  | 1 | 0 | 1 |
|  | 2 | 0 | 1 |
| 5 | 3 | - | - |
| 1 | 4 | - | - |
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| :---: | :---: | :---: | :---: |
|  | 0 | - | 0 |
| 4 | 1 | 0 | 1 |
|  | 2 | 0 | 1 |
| 3 | 3 | 2 | 2 |
|  | 4 | 2 | 2 |
| 5 | 5 | 0 | 1 |
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| 4 | 2 | 0 | 1 |
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